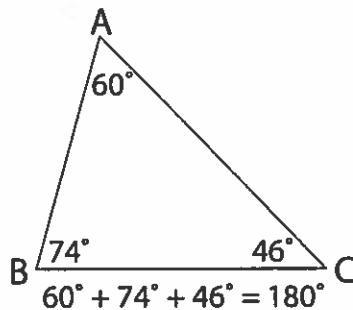


Investigating Angles in a Triangle

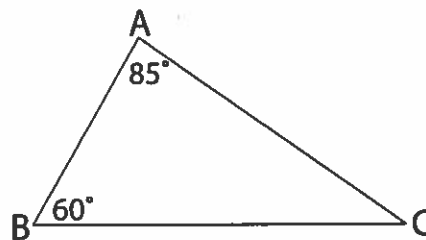


Quick Review

- The sum of the interior angles in a triangle is 180° .

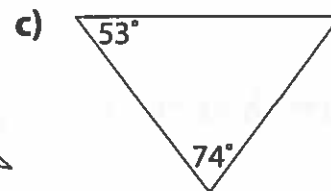
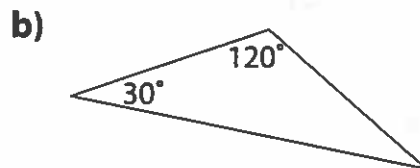
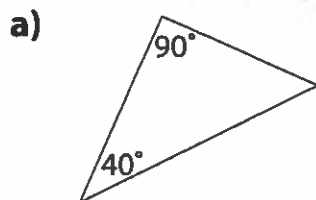


- To find the measure of $\angle C$ in triangle ABC:
 $\angle A + \angle B + \angle C = 180^\circ$
 Since $\angle A = 85^\circ$ and $\angle B = 60^\circ$,
 $85^\circ + 60^\circ + \angle C = 180^\circ$
 $145^\circ + \angle C = 180^\circ$
 $180^\circ - 145^\circ = 35^\circ$
 So, the measure of $\angle C$ is 35° .



Try These

- Determine the measure of the third angle without measuring.



- Two angles of a triangle are given. Find the measure of the third angle. Show your work.

a) $70^\circ, 60^\circ$ _____

b) $25^\circ, 90^\circ$ _____

c) $110^\circ, 40^\circ$ _____

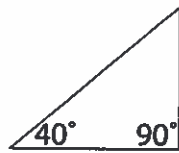
Practice

1. Determine if a triangle can be drawn with the angle measures given.
If a triangle can be drawn, draw and label it.

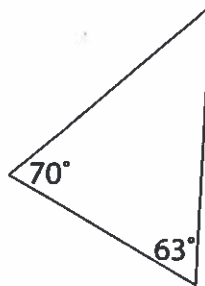
a) $35^\circ, 65^\circ, 80^\circ$ b) $55^\circ, 50^\circ, 50^\circ$ c) $45^\circ, 45^\circ, 90^\circ$ d) $95^\circ, 45^\circ, 50^\circ$

2. Determine the measure of the third angle without measuring.

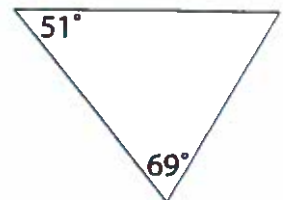
a)



b)



c)



3. Two angles of a triangle are given.
Find the measure of the third angle.

a) $62^\circ, 85^\circ$ _____ b) $60^\circ, 25^\circ$ _____ c) $37^\circ, 90^\circ$ _____

Stretch Your Thinking

Can you construct triangle DEF? Explain.

$$\angle D = 109^\circ$$

$$\angle E = 60^\circ$$

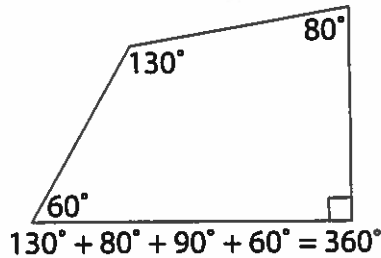
$$\angle F = 12^\circ$$

Investigating Angles in a Quadrilateral



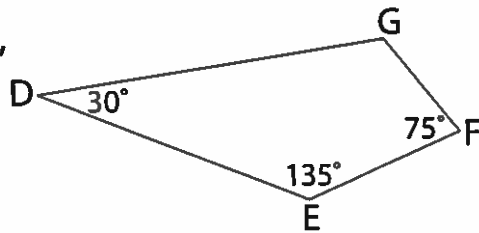
Quick Review

- ▶ The sum of the interior angles in a quadrilateral is 360° .



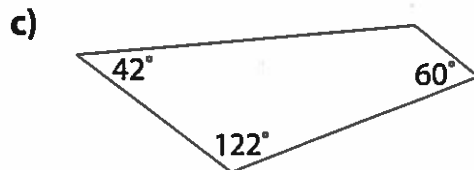
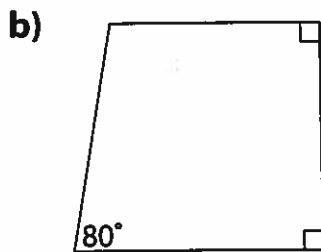
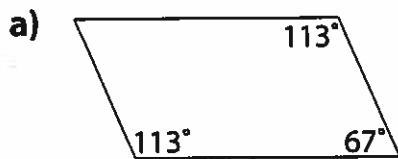
- ▶ To find the measure of $\angle G$ in quadrilateral DEFG:

$\angle D + \angle E + \angle F + \angle G = 360^\circ$
 Since $\angle D = 30^\circ$, $\angle E = 135^\circ$, and $\angle F = 75^\circ$,
 $30^\circ + 135^\circ + 75^\circ + \angle G = 360^\circ$
 $240^\circ + \angle G = 360^\circ$
 $360^\circ - 240^\circ = 120^\circ$
 So, the measure of $\angle G$ is 120° .



Try These

1. Determine the measure of the fourth angle without measuring.



2. Three angles of a quadrilateral are given. Find the measure of the fourth angle.

- | | |
|--|--|
| a) $25^\circ, 70^\circ, 110^\circ$ _____ | b) $42^\circ, 38^\circ, 100^\circ$ _____ |
| c) $90^\circ, 90^\circ, 41^\circ$ _____ | d) $115^\circ, 95^\circ, 63^\circ$ _____ |
| e) $107^\circ, 36^\circ, 49^\circ$ _____ | f) $116^\circ, 72^\circ, 49^\circ$ _____ |

Practice

1. Determine if a quadrilateral can be drawn with the angle measures given. If a quadrilateral can be drawn, draw and label it.

a) $90^\circ, 75^\circ, 60^\circ, 135^\circ$

b) $50^\circ, 45^\circ, 70^\circ, 120^\circ$

c) $125^\circ, 70^\circ, 85^\circ, 80^\circ$

2. Find the measure of the fourth angle in each quadrilateral.

Quadrilateral	$\angle J$	$\angle K$	$\angle L$	$\angle M$
A	149°	80°	26°	
B	120°	75°	97°	
C	76°	75°	84°	
D	150°	100°	70°	
E	37°	83°	151°	

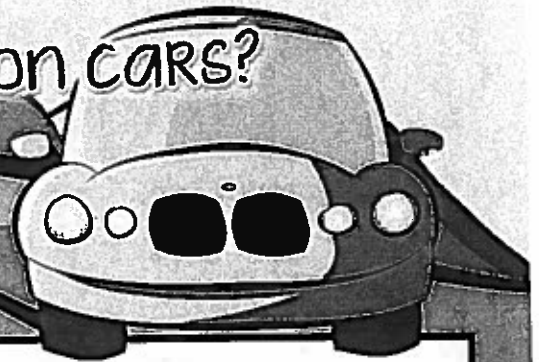
Stretch Your Thinking

Is it possible to make a quadrilateral with 3 obtuse angles and 1 right angle? Explain.

NAME: _____

DATE: _____

Why did the pencil like working on cars?



Solve the following problems in the sections below. Then record the corresponding letter of the correct answer in the rectangles at the bottom to answer the riddle.
Note: The problem numbers match the numbered rectangles.

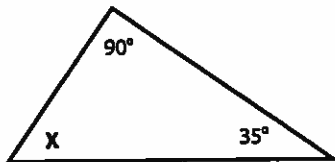
- ① A triangle's angles total _____ degrees.
B 360 **S** 180 **R** 90 **L** 100

- ② A quadrilateral's angles total _____ degrees.
P 360 **K** 180 **M** 90 **R** 100

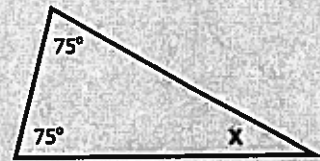
- ③ A triangle has three equal angles. What do they measure?
A 45° **N** 60° **Z** 90° **C** 100°

- ④ A parallelogram has two angles that each measure 25°. What must the other two angles each measure?
B 90° **G** 110° **W** 155° **H** 310°

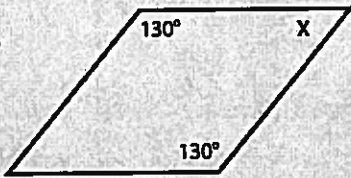
- ⑤ Find angle X: _____
G 45° **N** 60°
M 55° **Q** 100°



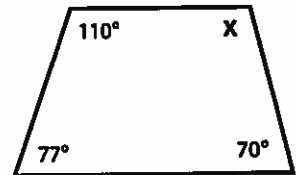
- ⑥ Find angle X: _____
F 5° **V** 10°
H 30° **A** 110°



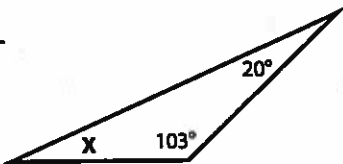
- ⑦ Find angle X: _____
L 50° **R** 90°
S 130° **D** 155°



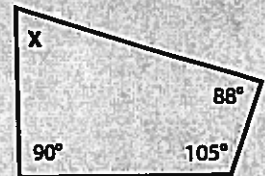
- ⑧ Find angle X: _____
A 77° **G** 91°
I 103° **U** 215°



- ⑨ Find angle X: _____
I 15° **O** 36°
A 57° **P** 112°



- ⑩ Find angle X: _____
S 12° **L** 90°
P 68° **C** 77°



- ⑪ Find angle X: _____
I 75° **E** 90°
O 180° **U** 200°



6	11

4	9	1

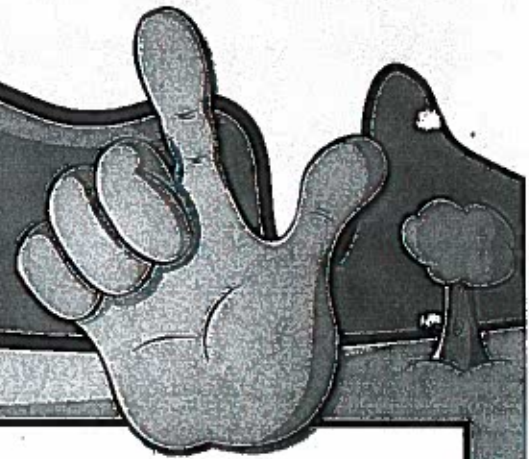
9

5	11	10	6	9	3	8	10	9	7

2	11	3	10	8	7

Skill: Finding unknown angles in triangles and quadrilaterals

Why was the index finger upset about not being in charge?



Solve the following problems in the sections below. Then record the corresponding letter of the correct answer in the rectangles at the bottom to answer the riddle.

Note: The problem numbers match the numbered rectangles.

Find the missing angle for problems 1–12:

1 **K** 21°
R 31°
S 121°
D 29°

2 **K** 29°
B 35°
N 68°
R 209°

3 **Q** 35°
P 45°
M 135°
A 305°

4 **T** 20°
S 40°
F 60°
E 90°

5 **N** 33°
T 14°
P 100°
D 107°

6 **F** 45°
N 55°
E 60°
L 90°

7 **I** 76°
O 84°
U 104°
M 93°

8 **S** 36°
M 97°
B 117°
N 207°

9 **D** 86°
C 90°
F 106°
W 130°

10 **S** 27°
T 47°
R 51°
H 57°

11 **W** 34°
B 54°
M 64°
H 74°

12 **E** 105°
A 115°
I 135°
O 205°

13 A ladder is leaning against a wall of a building. The ladder makes a 57° angle with the ground. What angle does it make with the building?

14 Three angles of a trapezoid measure 100°, 90°, and 75°. What is the measure of the other angle?

I 23°

E 33°

O 57°

P 123°

E 85°

U 95°

O 115°

I 175°

11	13	9	12	9	5	10	6	12	2	13	10	11	13	1	14	6	13	7	4	10	11	14	3	8
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Skill: Finding unknown angles in triangles and quadrilaterals